

**Topics :** Fundamentals of Mathematics, Sequence & Series, Trigonometric Ratio, Matrices & Determinants, Binomial Theorem, Straight Line, Permutation & Combination, Complex Number, Circle, Ellipse, Set & Relation

Type of Questions	M.M., Min.
Single choice Objective (no negative marking) Q.1 to Q.13 (3 marks, 3 min.)	[39, 39]
Assertion and Reason (no negative marking) Q.14, 15 (3 marks, 3 min.)	[6, 6]

- The equation  $e^{\sin x} - e^{-\sin x} - 4 = 0$  has :  
 (A) infinite number of real roots (B) no real roots  
 (C) exactly one real root (D) exactly four real roots
- Let  $A = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{pmatrix}$ . If  $u_1$  and  $u_2$  are column matrices such that  $Au_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$  and  $Au_2 = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$ , then  $u_1 + u_2$  is equal to:  
 (A)  $\begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$  (B)  $\begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$  (C)  $\begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}$  (D)  $\begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}$
- If  $n$  is a positive integer, then  $(\sqrt{3} + 1)^{2n} - (\sqrt{3} - 1)^{2n}$  is :  
 (A) an irrational number (B) an odd positive integer  
 (C) an even positive integer (D) a rational number other than positive integers
- If 100 times the 100<sup>th</sup> term of an AP with non zero common difference equals the 50 times its 50<sup>th</sup> term, then the 150<sup>th</sup> term of this AP is :  
 (A) - 150 (B) 150 times its 50<sup>th</sup> term  
 (C) 150 (D) zero
- In a  $\Delta PQR$ , if  $3 \sin P + 4 \cos Q = 6$  and  $4 \sin Q + 3 \cos P = 1$ , then the angle  $R$  is equal to :  
 (A)  $\frac{5\pi}{6}$  (B)  $\frac{\pi}{6}$  (C)  $\frac{\pi}{4}$  (D)  $\frac{3\pi}{4}$
- If the line  $2x + y = k$  passes through the point which divides the line segment joining the points  $(1, 1)$  and  $(2, 4)$  in the ratio  $3 : 2$ , then  $k$  equals :  
 (A)  $\frac{29}{5}$  (B) 5 (C) 6 (D)  $\frac{11}{5}$
- Assuming the balls to be identical except for difference in colours, the number of ways in which one or more balls can be selected from 10 white, 9 green and 7 black balls is :  
 (A) 880 (B) 629 (C) 630 (D) 879

8. If  $z \neq 1$  and  $\frac{z^2}{z-1}$  is real, then the point represented by the complex number  $z$  lies :  
 (A) either on the real axis or on a circle passing through the origin.  
 (B) on a circle with centre at the origin.  
 (C) either on the real axis or on a circle not passing through the origin.  
 (D) on the imaginary axis.
9. Let  $P$  and  $Q$  be  $3 \times 3$  matrices  $P \neq Q$ . If  $P^3 = Q^3$  and  $P^2Q = Q^2P$ , then determinant of  $(P^2 + Q^2)$  is equal to :  
 (A)  $-2$  (B)  $1$  (C)  $0$  (D)  $-1$
10. The length of the diameter of the circle which touches the  $x$ -axis at the point  $(1, 0)$  and passes through the point  $(2, 3)$  is :  
 (A)  $\frac{10}{3}$  (B)  $\frac{3}{5}$  (C)  $\frac{6}{5}$  (D)  $\frac{5}{3}$
11. Let  $X = \{1, 2, 3, 4, 5\}$ . The number of different ordered pairs  $(Y, Z)$  that can be formed such that  $Y \subseteq X, Z \subseteq X$  and  $Y \cap Z$  is empty, is :  
 (A)  $5^2$  (B)  $3^5$  (C)  $2^5$  (D)  $5^3$
12. An ellipse is drawn by taking a diameter of the circle  $(x - 1)^2 + y^2 = 1$  as its semi-minor axis and a diameter of the circle  $x^2 + (y - 2)^2 = 4$  as semi-major axis. If the centre of the ellipse is at the origin and its axes are the coordinate axes, then the equation of the ellipse is :  
 (A)  $4x^2 + y^2 = 4$  (B)  $x^2 + 4y^2 = 8$  (C)  $4x^2 + y^2 = 8$  (D)  $x^2 + 4y^2 = 16$
13. A line is drawn through the point  $(1, 2)$  to meet the coordinate axes at  $P$  and  $Q$  such that it forms a triangle  $OPQ$ , where  $O$  is the origin. If the area of the triangle  $OPQ$  is least, then the slope of the line  $PQ$  is :  
 (A)  $-\frac{1}{4}$  (B)  $-4$  (C)  $-2$  (D)  $-\frac{1}{2}$
14. **Statement-1** : The sum of the series  $1 + (1 + 2 + 4) + (4 + 6 + 9) + (9 + 12 + 16) + \dots + (361 + 380 + 400)$  is 8000.  
**Statement-2** :  $\sum_{k=1}^n (k^3 - (k-1)^3) = n^3$ , for any natural number  $n$ .  
 (A) Statement-1 is false, Statement-2 is true.  
 (B) Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for Statement-1.  
 (C) Statement-1 is true, statement-2 is true; statement-2 is **not** a correct explanation for Statement-1.  
 (D) Statement-1 is true, statement-2 is false.
15. **Statement-1** : An equation of a common tangent to the parabola  $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$  is  $y = 2x + 2\sqrt{3}$ .  
**Statement-2** : If the line  $y = mx + \frac{4\sqrt{3}}{m}$ , ( $m \neq 0$ ) is a common tangent to the parabola  $y^2 = 16\sqrt{3}x$  and the ellipse  $2x^2 + y^2 = 4$ , then  $m$  satisfies  $m^4 + 2m^2 = 24$ .  
 (A) Statement-1 is false, Statement-2 is true.  
 (B) Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for Statement-1.  
 (C) Statement-1 is true, statement-2 is true; statement-2 is **not** a correct explanation for Statement-1.  
 (D) Statement-1 is true, statement-2 is false.

# Answers Key

- |         |         |         |         |
|---------|---------|---------|---------|
| 1. (B)  | 2. (D)  | 3. (A)  | 4. (D)  |
| 5. (B)  | 6. (C)  | 7. (D)  | 8. (A)  |
| 9. (C)  | 10. (A) | 11. (B) | 12. (D) |
| 13. (C) | 14. (B) | 15. (B) |         |

